
Internal Dosimetry from Radionuclides Intakes

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Content I

- Dose (some definitions)
- Biokinetics (Compartment model)
- HRTM
- HAT
- Wound model
- Monitoring Internal contamination
- From measurements to Intake

Content II

- General Guidelines for the Assessment of Internal Dose from monitoring Data. (project IDEAS)
- Examples
 - Acute Inhalation of ^{60}Co
 - Acute Inhalation of fission products: ^{90}Sr
 - Acute Inhalation of Plutonium

Absorbed Dose

- The physical dose quantity given by

$$D = \frac{d \bar{\varepsilon}}{d m}$$

- $d\varepsilon$ = mean energy imparted by ionisation radiation to the matter in a volume element
- dm = the mass of the matter in this volume element
- SI unit is joule per kilogram (J kg^{-1}) = gray (Gy)

~~Equivalent~~ Radiation weighted Dose ($H_{T,R}$)

- Equivalent Radiation weighted Dose in tissue or organ T due to radiation R

$$H_{T,R} = w_R \bullet D_{T,R}$$

- $D_{T,R}$ = the average absorbed dose from radiation R in tissue T
- w_R = the radiation weighting factor based on the quality of the radiation emitted by the source.
- SI unit = $J\ kg^{-1}$ = sievert (Sv)

Radiation weighting factors (w_R) ICRP 60

| Type and energy range | Radiation weighting factor (w_R) |
|---|--------------------------------------|
| Photons, gamma | 1 |
| Electrons, Beta | 1 |
| Neutrons, energy from < 10 keV to > 20 MeV | 5 - 20 |
| Protons | 5 2 |
| Alpha particles, fission fragments, heavy nuclei | 20 |

~~Total equivalent~~ Radiation weighted Dose (H_T)

- The sum of $H_{T,R}$ over all radiation types

$$H_T = \sum_R H_{T,R}$$

Effective Dose (E)

- The sum of the weighted ~~equivalent~~ radiation weighted doses in all tissues and organs of the body.

$$E = \sum_T w_T \cdot H_T$$

- w_T = tissue weighting factor
- H_T = ~~equivalent~~ radiation weighted dose for tissue or organ T

Tissue weighting factor

| Organ or Tissue (T) | Tissue weighting factor (w_T) |
|---|-----------------------------------|
| Gonads | 0.20 0.05 |
| Bone marrow (red), Colon, Lung, Stomach, Breast | 0.12 |
| Bladder, Breast , Liver, Oesophagus, Thyroid | 0.05 |
| Skin, Bone surface, Brain , Kidney , Salivary glands | 0.01 |
| Remainder | 0.05 0.10 |

Committed equivalent dose ($H_T(\tau)$)

- The time integral of the equivalent dose rate in a particular tissue or organ that will be received by an individual following intake of radioactive material into the body, where t is the integration time in years following the intake.

$$H_T(\tau) = \int_{t_0}^{t_0 + \tau} H_T(t) dt$$

- For adults, the integration time is 50 year

Committed equivalent dose ($H_T(50)$)

$$H_T(50) = \sum_S U_S(50) \cdot SEE(T \leftarrow S)$$

- $U_S(50)$ = number of nuclear transformations (Bq s) in 50 y in source S following acute intake
- $SEE(T \leftarrow S)$ = Specific Effective Energy, equivalent dose in T per transformation in S expressed as ($\text{Sv}(\text{Bq s})^{-1}$)

Specific Effective Energy

$$SEE(T \leftarrow S) = \sum_R \frac{Y_R E_R w_R AF(T \leftarrow S)_R}{m_T}$$

- Y_R = yield of radiation R per nuclear transformation
- E_R = energy of radiation R (J)
- w_R = radiation weighting factor for radiation R
- $AF(T \leftarrow S)_R$ = absorbed fraction in T per transformation in S for radiation R
- m_T = mass of the target tissue, T (kg)

Committed Effective Dose

- The sum of the product of the committed equivalent doses in organs or tissues and the appropriate organ or tissues weighing factor (w_T) where τ is the integration time in time following the intake.

$$E(\tau) = \sum_T w_T \cdot H_T(\tau)$$

- For adults, the integration time is 50 year

Dose coefficient

- $h_T(\tau)$ = committed tissue equivalent dose per unit acute intake
- $e(\tau)$ = committed effective dose per unit acute intake
- Where τ is the time period in years over which the dose is calculated
- Example : ^{239}Pu Type S, $e(50) = 8.3 \cdot 10^{-6} \text{ Sv Bq}^{-1}$

Dose limits

- The occupational exposure of any worker shall be so controlled that the following limits be not exceeded:
 - an **effective dose of 20 mSv** per year averaged over five consecutive years;
 - an **effective dose of 50 mSv** in any single year;
 - an **equivalent dose to the lens of the eye of 150 mSv** in a year;
 - an **equivalent dose to the extremities (hands and feet) or the skin of 500 mSv** in a year.

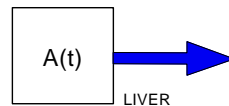
Biokinetics

Introduction to compartment models

Biokinetic behaviour

- Route of intake (ingestion, inhalation, injection ...)
- Accumulation of activity in specific organs
- Retention of radionuclides in those organs
- Transport of radionuclides between organs
- Removal, by excretion and radioactive decay, of activity from the body

Transport out of a compartment



$$A(t) = A_0 e^{-\alpha t}$$

Uptake

- Material which is absorbed from the respiratory tract or the gastro-intestinal tract first enter the blood or lymph (body fluids) and is then available for uptake by organs.

Compartment model for uptake

- From the transfer compartment with half-time 6 hours (for most radionuclides)
- 30 % to Organ 1, 70 % to Organ 2

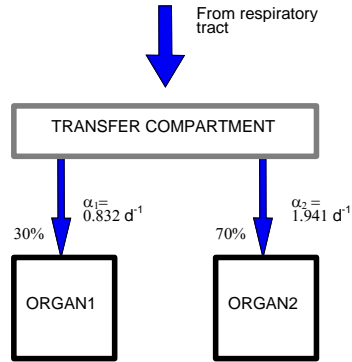
$$\frac{\alpha_1}{\alpha_2} = \frac{3}{7}$$

$$\alpha_1 + \alpha_2 = \frac{\ln(2)}{0.25} \quad (d^{-1})$$

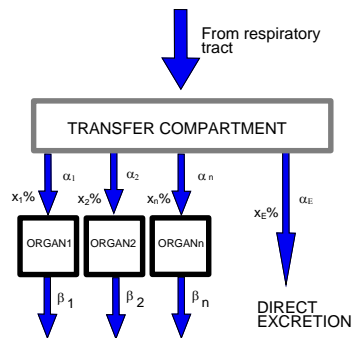
$$\alpha_1 = 0.832 \quad (d^{-1})$$

$$\alpha_2 = 1.941 \quad (d^{-1})$$

Compartment model for uptake

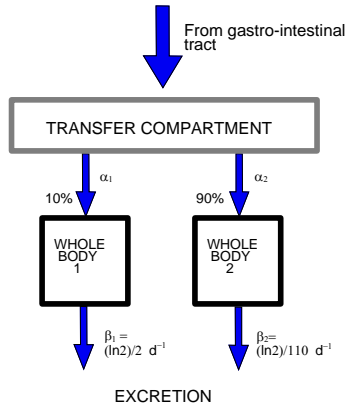


Compartment model for retention

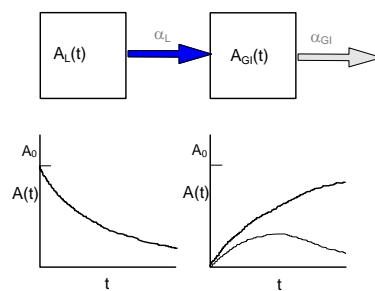


$$R(t) = \frac{A(t)}{A_0} = e^{-\alpha t}$$

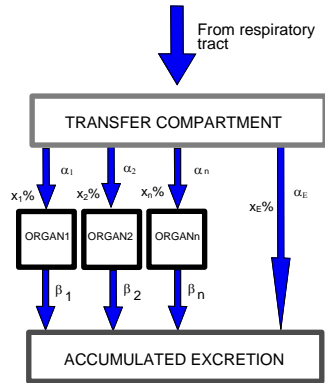
Model for caesium retention



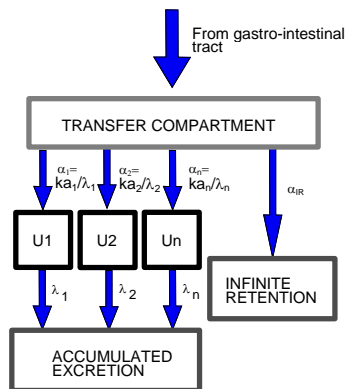
Model for transport between organs



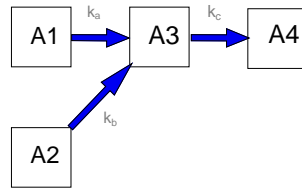
Model for excretion



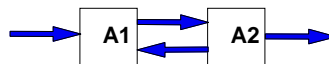
Model for an excretion function



Multiple path compartment model



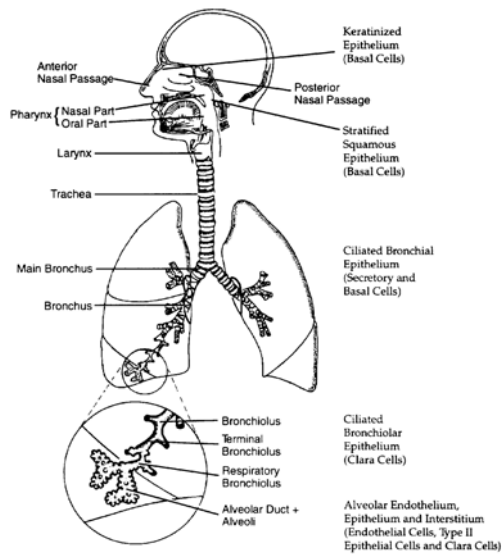
Recycling compartment model



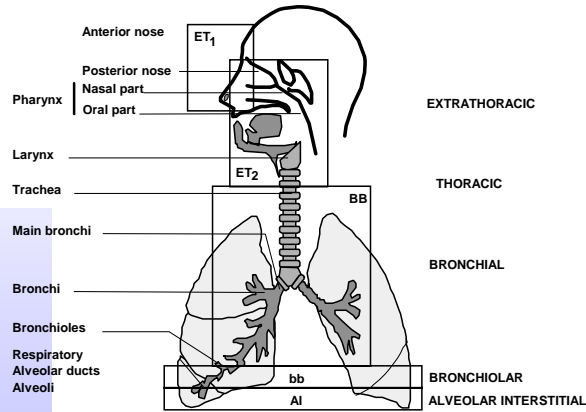
Human Respiratory Tract Model

ICRP Publication 66

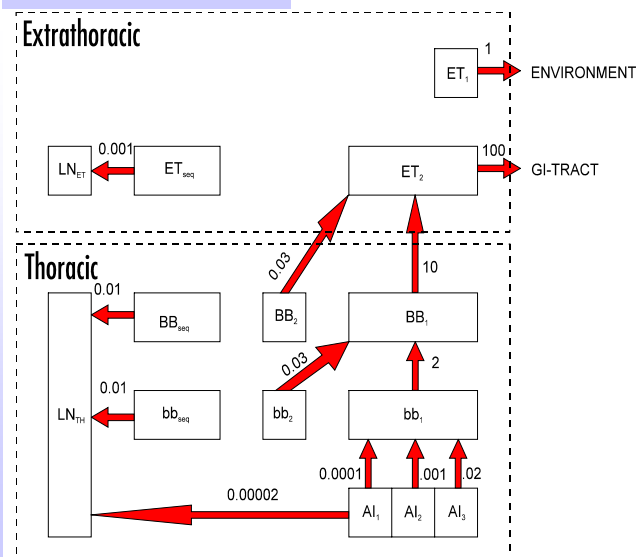
Human Respiratory Tract



Human Respiratory Tract



Particle transport in the human respiratory tract



$$\frac{\Delta k_{eff}}{(\Delta R)^2 \sigma_g} \left[\left(1 + \frac{\sigma_g}{\lambda}\right) T_{m+n} - \left(2 + \frac{\sigma_g}{\lambda}\right) T_{m+n} + T_{m+n-1} \right] - \rho \beta \frac{\Delta k_{eff} T_{m+n} + T_{m+n-1}}{C_{eff}}$$



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Deposition (I)

- Deposition model evaluates fractional deposition of the aerosol in each region for all particle sizes of practical interest (0.0006 – 100 μm)
- Aerosols:
 - Activity Median Aerodynamic Diameter = AMAD
 - Lognormal particle size distribution
 - Geometric standard deviation (σ_g) function of the median particle size
 - = 1.0 at 0.0006 μm
 - = 2.5 at 1 μm and above

Deposition (II)

- Exposure : Occupational or environmental
- Male or Female, adult or child or infant or baby
- Activities
 - Sleep
 - Sitting
 - Light exercises
 - Heavy exercises
- Nose and/or mouth breather

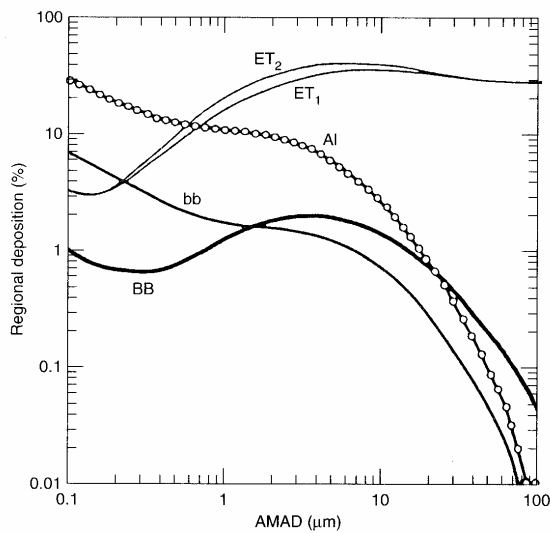
Deposition (III)

- Standard worker (ventilation rate = 1.200 m³/h)
 - Sleep 0 %
 - Sitting 31.3 %
 - Light exercises 68.8 %
 - Heavy exercises 0 %
- Heavy worker (ventilation rate = 1.688 m³/h)
 - Sleep 0 %
 - Sitting 0 %
 - Light exercises 87.5 %
 - Heavy exercises 12.5 %

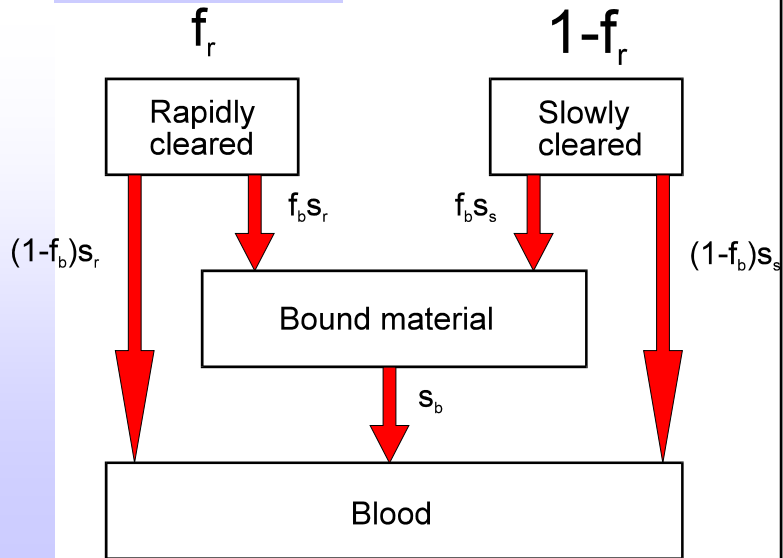
Deposition of inhaled aerosols

| Region | AMAD 1 μm | AMAD 5 μm |
|-----------------|----------------------|----------------------|
| ET ₁ | 16.5 | 33.9 |
| ET ₂ | 21.1 | 39.9 |
| BB | 1.24 | 1.78 |
| bb | 1.65 | 1.10 |
| AI | 10.7 | 5.3 |
| Total | 51.2 | 82.0 |

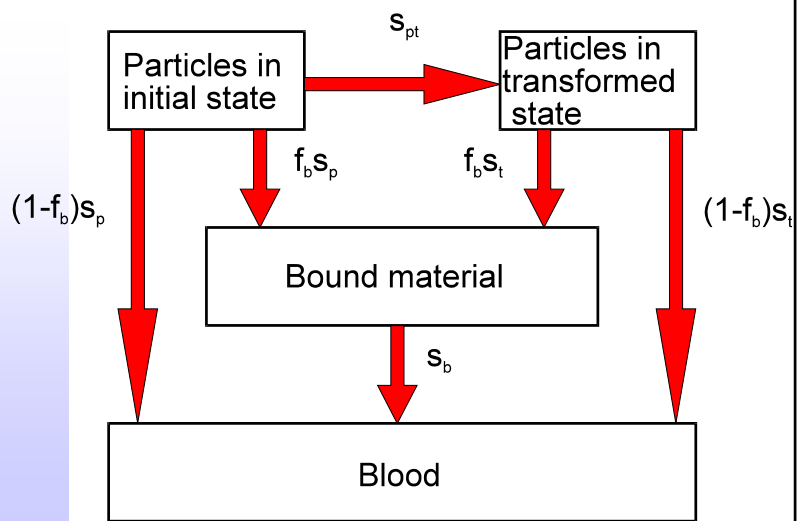
Regional deposition % in function of AMAD



Compartmental representation of absorption to blood (I)



Compartmental representation of absorption to blood (II)



Absorption rate

- If known used absorption rate for specific compound
- Default values for three material
 - Type F (fast)
 - Type M (moderate)
 - Type S (slow)

Type F (fast)

- 100 % absorbed with a half-time of 10 minutes.
- There is rapid absorption of almost all material deposited in BB, bb, and AI,
- and 50% of material deposited in ET₂ is clear to the GI tract by particle transport.
- Example: all compounds of Cs and I

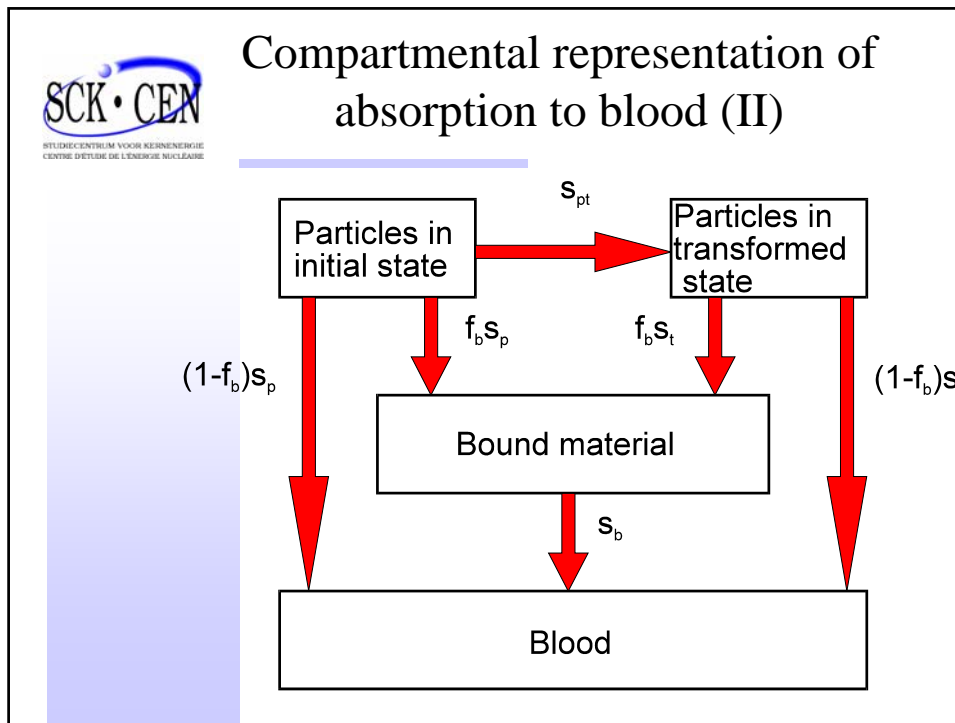
Type M (moderate)

- 10% absorbed with a half-life of 10 minutes and 90% with a half-life of 140 d.
- There is rapid absorption of about 10% of the deposit in BB and bb; and 5% of material deposited in ET2.
- About 70% of the deposit in AI eventually reaches the body fluids.
- Example: all compounds of Ra and Am

Type S (slow)

- 0.1% absorbed with a half-life of 10 minutes and 99.9% with a half-life of 7000 d.
- There is little absorption from ET, BB, or bb;
- about 10% of the deposit in AI eventually reaches the body fluids.
- Examples: all insoluble compounds of U and Pu

Compartmental representation of absorption to blood (II)



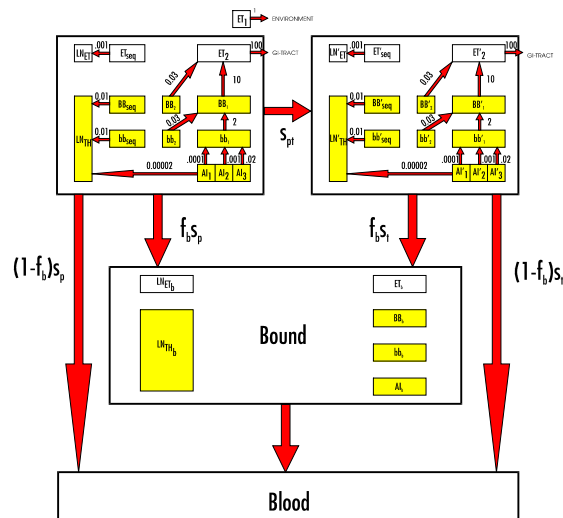
Default absorption parameters

| Model parameters (d^{-1}) | Type F | Type M | Type S |
|----------------------------------|--------|--------|--------|
| s_p | 100 | 10 | 0.1 |
| s_{pt} | 0 | 90 | 100 |
| s_t | - | 0.005 | 0.0001 |

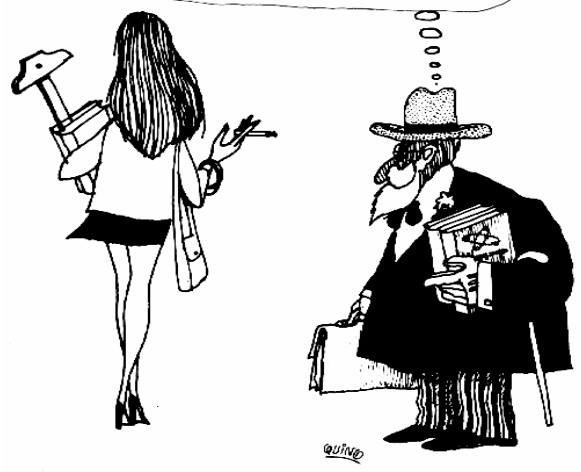
Absorption parameters for gas and vapour

- Absorptions Type F or V (Very rapid absorption)
- Class SR-0: Insoluble and non-reactive negligible deposition
 - ^{41}Ar , ^{85}Kr , ^{133}Xe
- Class SR-1: Soluble or reactive deposition may occur
 - Tritium (g), ^{14}CO , ^{131}I vapour, ^{195}Hg vapour
- Class SR-2: Highly soluble or reactive complete deposition in ET_2 for calculation = directly injected in blood
 - ^3H organic compounds and tritiated water

Full compartmental representation of absorption to blood



$$\frac{\Delta I_{\alpha}}{(AR)^2 G_{\alpha}} \left[\left(1 + \frac{\lambda}{\alpha}\right) T_{m+n} - \left(2 + \frac{\lambda}{\alpha}\right) T_{m+n-1} + T_{m+n-2} \right] - p \beta \frac{\Delta I_{\alpha}}{G_{\alpha}} \frac{T_{m+n} + T_{m+n-1}}{2} + f_{m+n} + \frac{\Delta I_{\beta}}{(AR)^2 G_{\beta}} \left[\left(1 + \frac{\lambda}{\beta}\right) f_{m+n} - \left(2 + \frac{\lambda}{\beta}\right) f_{m+n-1} + f_{m+n-2} \right] +$$



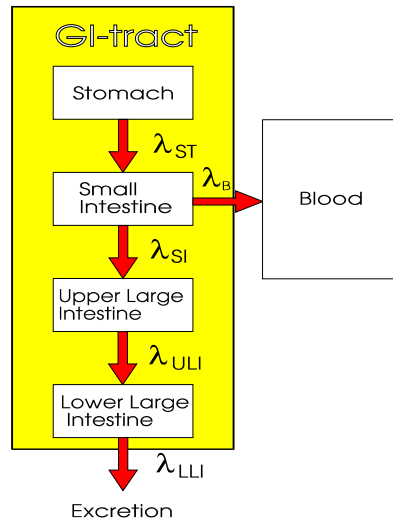
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Gastro-Intestinal Tract Model

ICRP Publication 30

GI Tract (ICRP 30)



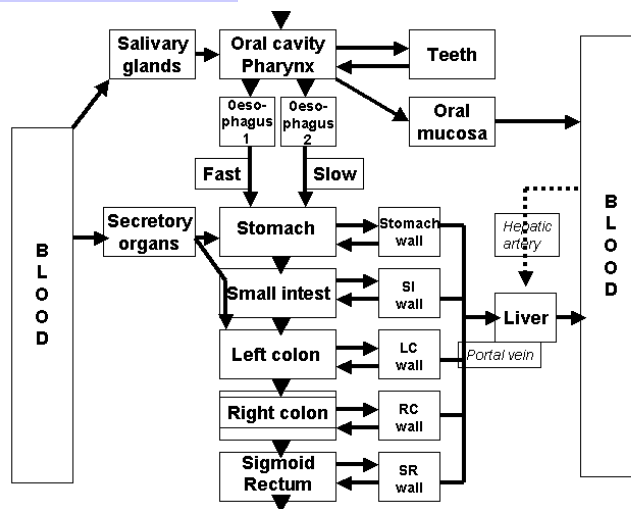
GI Tract compartments

- Stomach
 - Mean residence time = 1 hour
- Small Intestine
 - Mean residence time = 4 hours
 - Absorption to blood
 - Fraction of material reaching body fluids $f_1 = \frac{\lambda_B}{\lambda_B + \lambda_{SI}}$
 - SI is alkaline
- Upper large intestine
 - Mean residence time = 13 hours
- Lower large intestine
 - Mean residence time = 24 hours

Human Alimentary Tract Model

ICRP Publication ?? 2005

HAT Human Alimentary Tract



$$\frac{\Delta k_{\infty}}{(\Delta R)^2 G_{eff}} \left[\left(1 + \frac{\beta}{\lambda}\right) T_{mn} - \left(2 + \frac{\beta}{\lambda}\right) T_{m-1,n} + T_{m-2,n} \right] - \frac{\rho \beta \Delta L}{G_{eff}} \frac{\Delta H_{eff} T_{mn} + T_{m-1,n}}{2} + f_{m,n} + \frac{\Delta L \rho \beta}{(\Delta R)^2 G_{eff}} \left[\left(1 + \frac{\beta}{\lambda}\right) f_{m+1,n} - \left(2 + \frac{\beta}{\lambda}\right) f_{m,n} + f_{m-1,n} \right] + \frac{\partial T}{\partial L} - \frac{k_{\infty}}{G_{eff}} \left(2 \frac{\partial^2 T}{\partial R^2} \right) + \frac{\rho \beta \Delta H_{eff}}{G_{eff}} r + \frac{\Delta L \rho \beta}{(\Delta R)^2 G_{eff}} (f_{m-1,n} + \Delta L \rho \beta \left(\frac{\partial C}{\partial C} \right)_{0+}$$

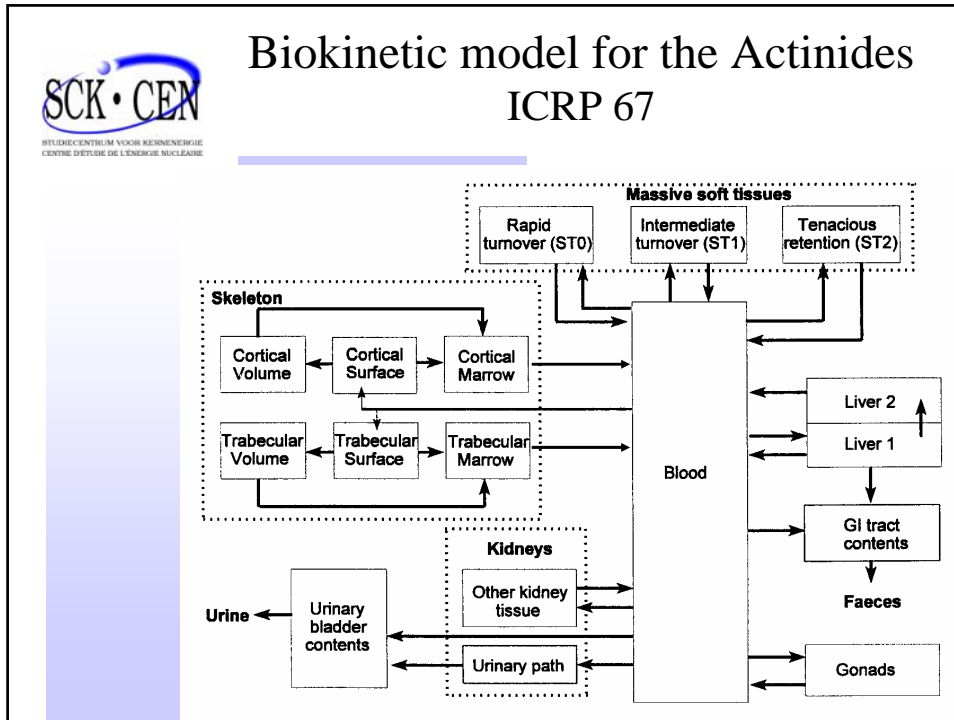


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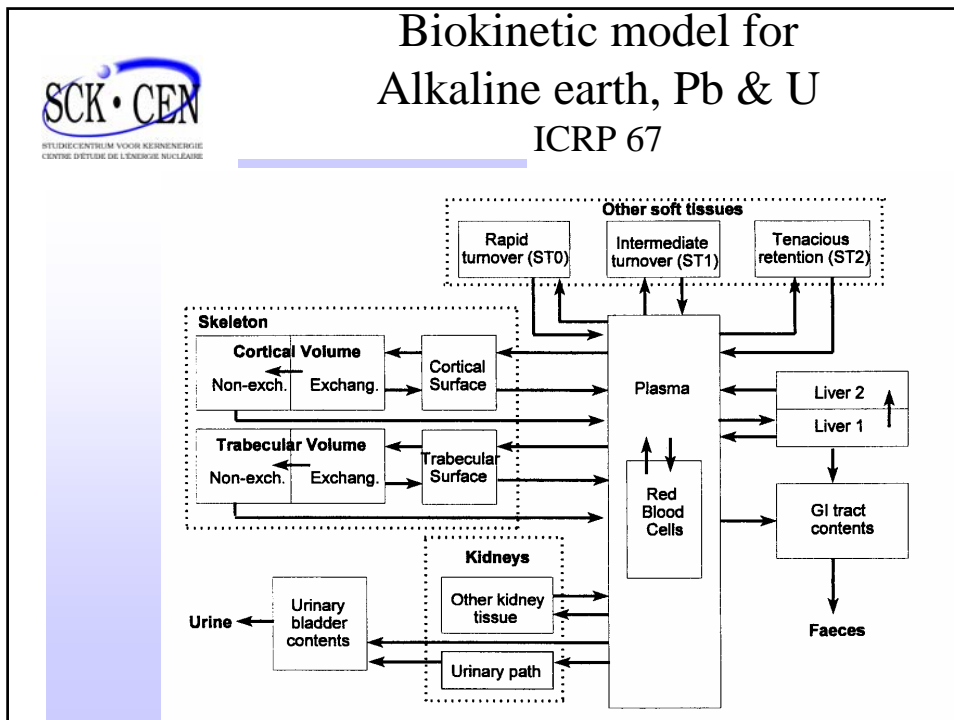
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Some biokinetic models

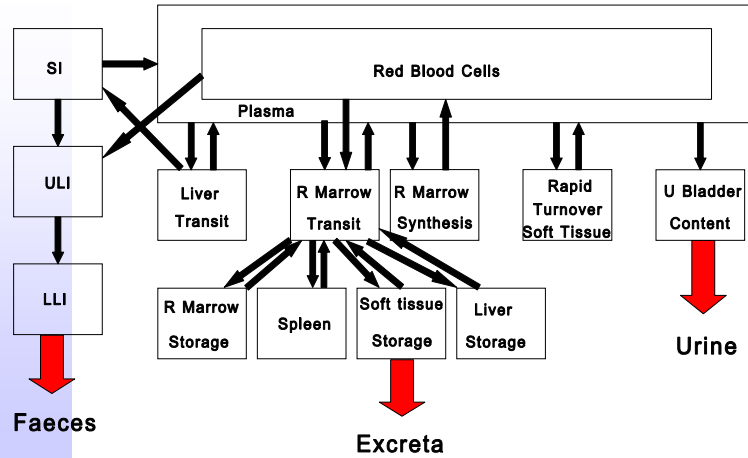
Biokinetic model for the Actinides ICRP 67



Biokinetic model for Alkaline earth, Pb & U ICRP 67



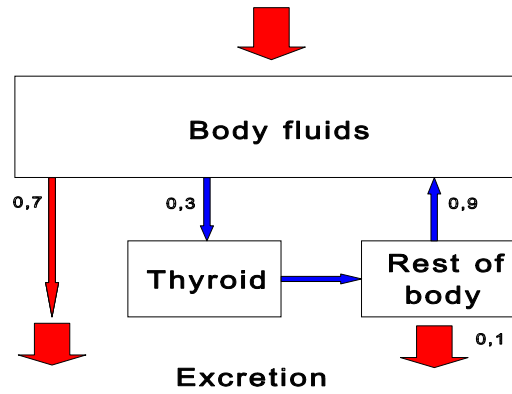
Biokinetic model for Iron ICRP 69



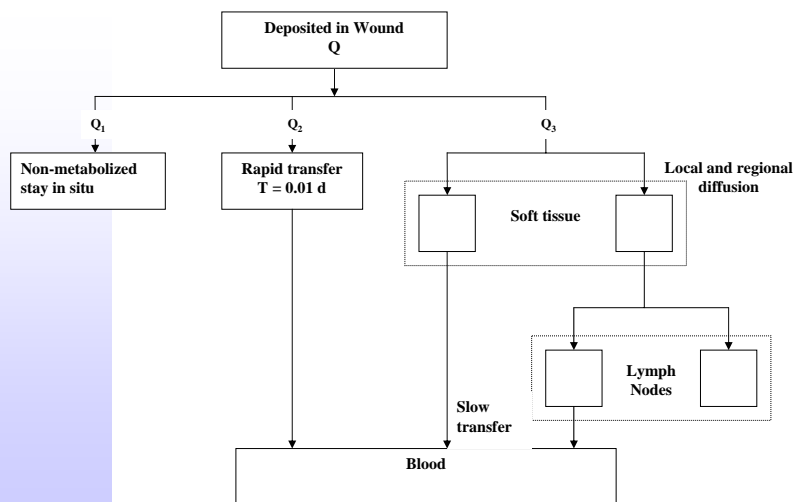
$$\frac{\Delta I_{e,t}}{(\Delta R)^2 G_{eff}} \left[\left(1 + \frac{1}{m}\right) T_{m+1,n} - \left(2 + \frac{1}{m}\right) T_{m,n} + T_{m-1,n} \right] - p_B \frac{\Delta L \Delta H r T_{m+1,n} + T_{m,n}}{G_{eff}} + f_{m,n} + \frac{\Delta L p_B p}{(\Delta R)^2 G} \left[\left(1 + \frac{1}{m}\right) f_{m+1,n} - \left(2 + \frac{1}{m}\right) f_{m,n} + f_{m-1,n} \right] + \frac{\Delta I}{\Delta L} - \frac{L_e}{G_{eff}} \left(2 \frac{\partial^2 T}{\partial R^2} \right) + p_B \frac{\Delta H r}{G_{eff}} + \frac{\Delta L \Delta H p}{(\Delta R)^2 G} (G_{m,n} - f_{m,n} + \Delta L p_B \frac{p}{G C})_0 + \frac{L_{m,n} + 1}{2} T_{m,n} - p_B \frac{\Delta L p_B \Delta H r}{G (\Delta R)^2} \left[\left(2 + \frac{2}{m}\right) f_{T,m-1,n} + \frac{T_{m,n} + 1}{\Delta G} \frac{\Delta L p_B G_2 - 1}{\Delta G} \right]$$



Biokinetic model for Iodine ICRP 30



Wound model (I)



Wound model (II)

- Q_1 = metabolically inert, it remains where it was deposited
- Q_2 = enters the bloodstream quickly via the vascular breaches
- Q_3 = diffuse slowly in the soft tissue (conjunctive tissue, muscles ..) from where it is finally transferred to the blood, either directly or indirectly via the lymph nodes.

$$\frac{\Delta k}{(\Delta R)^2 G_{ef}} \left[\left(1 + \frac{1}{m}\right) T_{m+1n} - \left(2 + \frac{1}{m}\right) T_{mn} + T_{m-1n} \right] - p_B \frac{\Delta L \Delta H T_{m+1n} + T_{m+1n}}{G_{ef}} +$$

$$+ f_{m,n} + \frac{\Delta L p_B}{(\Delta R)^2 G} \left[\left(1 + \frac{1}{m}\right) f_{m+1n} - \left(2 + \frac{1}{m}\right) f_{mn} + f_{m-1n} \right] +$$

$$+ \frac{\partial T}{\partial L} - \frac{k_e}{G_{ef}} \left(2 \frac{\partial^2 T}{\partial R^2} \right) + \frac{p_B \Delta H r}{G_{ef}} + \frac{\Delta L \Delta P}{(\Delta R)^2 G} (G_n - S_n + \Delta L p_B \frac{G}{G_{ef}}) +$$

$$+ \frac{T_{m+1n} + T_{1n}}{2} - p_B \frac{\Delta L m - 2n H_e}{G (\Delta R)^2} \left[\left(2 + \frac{2}{m}\right) f_{1n} - m - 1n + \frac{T_{m+1n} \Delta L p_B G_{2-1n}}{\Delta G_{ef}} \right]$$

$$+ \frac{\Delta P}{L} - \frac{2 P D_2^2 \lambda^2}{\sqrt{A p e^3}} \theta = \frac{N D_p}{H N r} =$$



$$\frac{\Delta L_e}{(\Delta R)^2 G_f} \left[\left(1 + \frac{1}{m}\right) T_{m+n} - \left(2 + \frac{1}{m}\right) T_m + T_{m-1} \right] - p \beta \frac{\Delta L_e}{G_f} \frac{T_{m+n} + T_m}{2} +$$

$$+ f_{m+n} + \frac{\Delta L_e p \beta}{(\Delta R)^2 G_f} \left[\left(1 + \frac{1}{m}\right) f_{m+n} - \left(2 + \frac{1}{m}\right) f_m + f_{m-1} \right] +$$

$$+ \frac{\Delta T}{\Delta L} - \frac{k_e}{G_f} \left(\frac{2 \Delta T}{\Delta R^2} \right) + \frac{p \beta \Delta H_e}{G_f} r + \frac{\Delta L_e p \beta}{(\Delta R)^2 G_f} (f_m - f_{m-1} + \Delta L p \beta \frac{p \beta}{G_f}) +$$

$$+ \frac{f_{m-1} + f_m}{2} - p \beta \frac{\Delta L_e p \beta}{G_f} \left[\left(1 + \frac{1}{m}\right) f_{m-1} - m - 1 \right] - \frac{T_{m+n} + 1 \Delta L_e p \beta G_f - 1}{\Delta G_f} +$$

$$+ \frac{\Delta P}{L} - \frac{2 P D_e^2 \rho}{\sqrt{A} \rho c^3} \phi = \frac{\Delta P}{H N_f} = \text{chair}$$

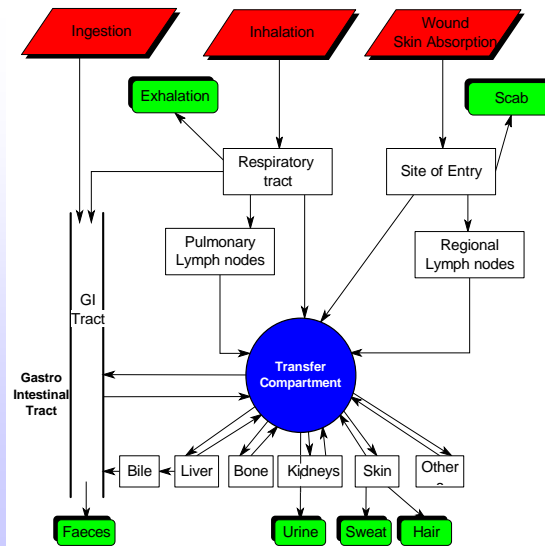


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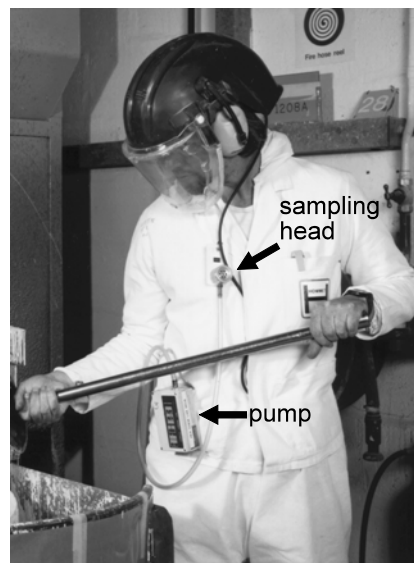
Monitoring Internal contamination

Routes of entry



Monitoring type (I)

- Air sampling
 - Static air sampler
 - ♣ localise
 - Portable air sampler
 - Personal air sampler PAS
 - ♣ Low sampling rate
 - ♣ Trigger biological monitoring



Monitoring type (II)

- Direct measurements - *in vivo* monitoring
 - Possible when the incorporated radionuclide emit penetrating radiation of sufficient energy and yield to be detectable outside the body (X ray or gamma photon)
- Indirect measurements – excreta measurements
 - organs & tissues concerned are not sampled
 - Knowledge of relationships between
 - ◆ bioassay samples
 - ◆ organ burdens of interest

Monitoring type

- Direct measurements
 - Whole body counting
 - Thyroid measurement
 - Lung counting
 - Wound counting
- Indirect measurements
 - Nose-blow
 - Urine
 - Faeces
 - Blood, hair, sweat, saliva ...

In vivo monitoring

Jean-Louis Genicot

Bioassay measurements

Types of Bioassay samples (I)

- Chemical element involved
- Physical & chemical form
- Magnitude of the internal deposition
- Biological & Physical half-lives of radionuclides involved
- Elapsed time since the deposition
- Sensitivity of analytical method

Types of Bioassay samples (II)

- Urine
 - ◆ most used
 - ◆ 24 hours sampling
 - ◆ at SCK-CEN 3 consecutive days (36h)
 - ◆ $^3\text{H}_2\text{O}$: a voiding
 - ◆ repetitive sampling



Types of Bioassay samples (III)

- Faeces
 - ♦ not often used for routine
 - ♦ accidental inhalation
- Nose-blow, Nose-swap
 - ♦ α emitters
 - ♦ triggers complementary analysis

Types of Bioassay samples (IV)

- blood
- sweat
- saliva
- hair
- teeth
- breath
 - ♦ $^{14}\text{CO}_2$, $^3\text{H}_2\text{O}$, ^{222}Rn , ^{220}Rn
- tissue
 - ♦ remove for medical purpose, post mortem

Radiochemical Procedure (I)

- Sample preparation & Pre-concentration
- Urine
 - ♦ wet ashing
 - ♦ co-precipitation
- Faeces
 - ♦ ashing
 - ♦ dissolution
 - ♦ HF treatment



Radiochemical Procedure (II)

- Chemical separation
 - ♦ ion-exchange resin
 - ♦ solvent extraction
 - ♦ combination
 - ♦ ...

Radiochemical Procedure (III)

- Source preparation
- α emitters
 - ♦ direct evaporation
 - ♦ co-precipitation with LnF
 - ♦ Electro-deposition
- β emitters
 - ♦ precipitation & filtration of insoluble salt
 - ♦ MgNH_4PO_4 , SrCO_3 , $\text{Y}_2(\text{C}_2\text{O}_4)_3$, PdI_2

Measuring Techniques

- α spectrometry
- β counting
- Liquid Scintillation Counting - LSC
- γ spectrometry
- Fluorimetry
- Neutron Activation Analysis - NAA
- Delay Neutron Assay - DNA
- Mass spectrometry - ICPMS, SIMS
- Fission Track Analysis

α spectrometry

- Th, U, Pu, Am, Cm...
- radiochemical procedure
- source preparation
 - ♦ co-precipitation LnF
 - ♦ electro-deposition
- Yield determinant
 - ♦ ^{229}Th , ^{232}U , ^{242}Pu , ^{243}Am
- MDA = 0.1 mBq/l

β Counting

- strong β emitters
 - ♦ ^{32}P , ^{89}Sr , ^{90}Sr , ^{90}Y , ^{131}I
- radiochemical procedure
- source: insoluble salt
- gas proportional counter - low background
- MDA = 0.08 Bq/l
for ^{90}Sr , urine sample of 250cc

Liquid Scintillation Counting LSC

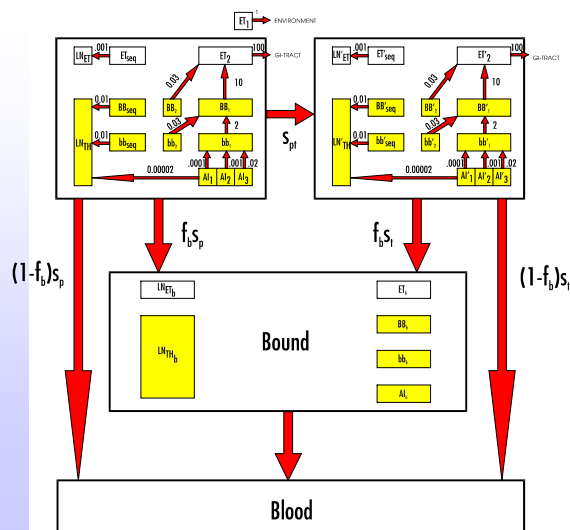
- weak energy β emitters - ^3H , ^{14}C , ^{63}Ni , ^{241}Pu
 - ◆ direct measurement
 - ◆ use of internal standard
 - ◆ MDA = 5 Bq/l for ^3H in urine (Vol. = 9 cc)
- pure β emitters - ^{32}P , ^{89}Sr , ^{90}Sr
 - ◆ radiochemical procedure
 - ◆ MDA = 0.12 Bq/l (Vol. = 600 cc)

γ Spectrometry

- direct measurement
- 250 cc sample
- MDA = 0.2 Bq/l
- *in-vivo* measurement
 - ◆ Whole-body
 - ◆ Thyroid

From measurements to Intake

Lung Model

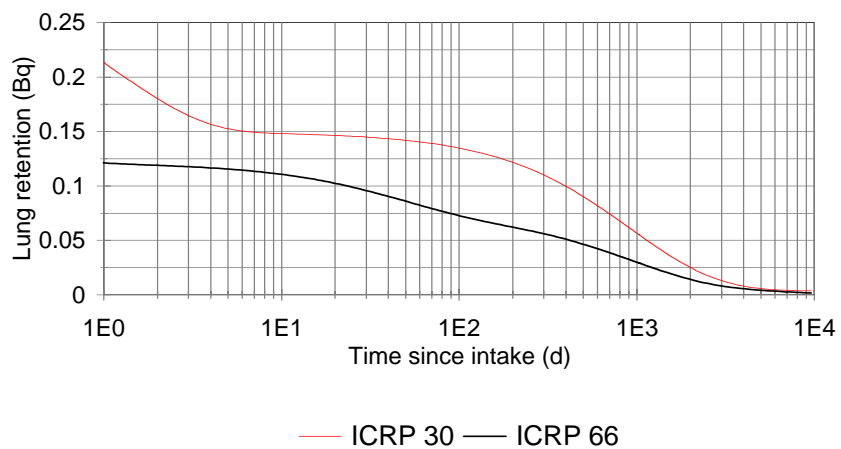


Lung Retention

- Calculate the retention of a radionuclide at times after inhalation
- Needed
 - AMAD
 - Solubility class
 - Lung Model (new) from ICRP 66
- Σ all the compartments
- Then...

Lung Retention ^{239}Pu Class Y acute inhalation $1\ \mu\text{m}$ AMAD

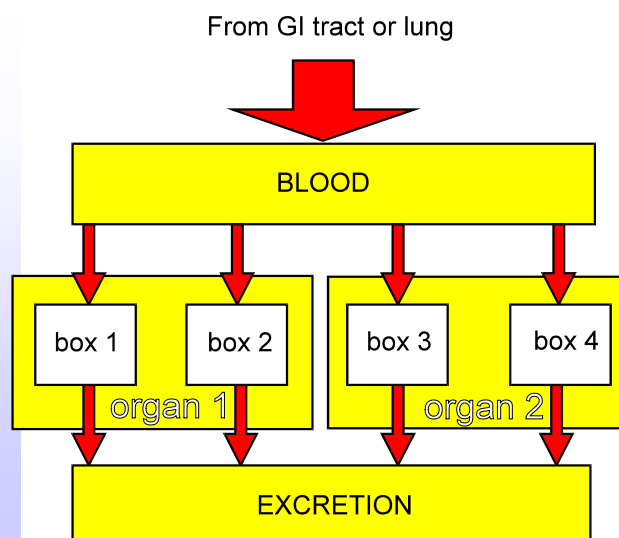
Lung retention following intake of Pu
 (1 Bq acute intake of Pu-239)



Whole body retention

- Total amount of activity in the body
- Includes activity retained
 - Respiratory tract
 - Alimentary tract (f_1)
 - Blood
 - Body organs
- Activity in body organs (excluding HAT & HRT)
= **systemic activity**

Simple biokinetic models



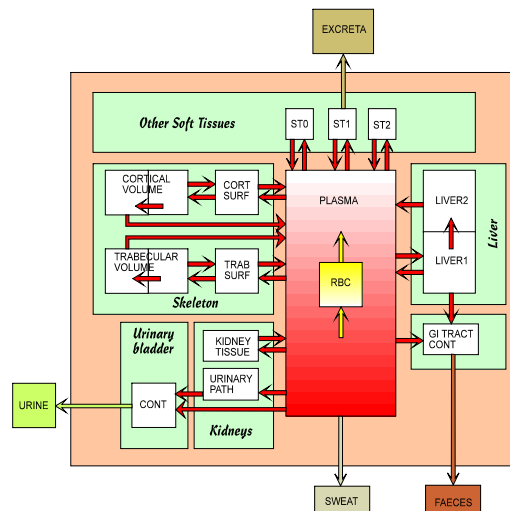
Systemic retention function

- Organ or tissue represented by a sum of exponential terms
- Whole body = sum of each organ = sum of exponential terms

$$R(t) = \sum_{i=1}^5 a_i e^{-\lambda_i t}$$

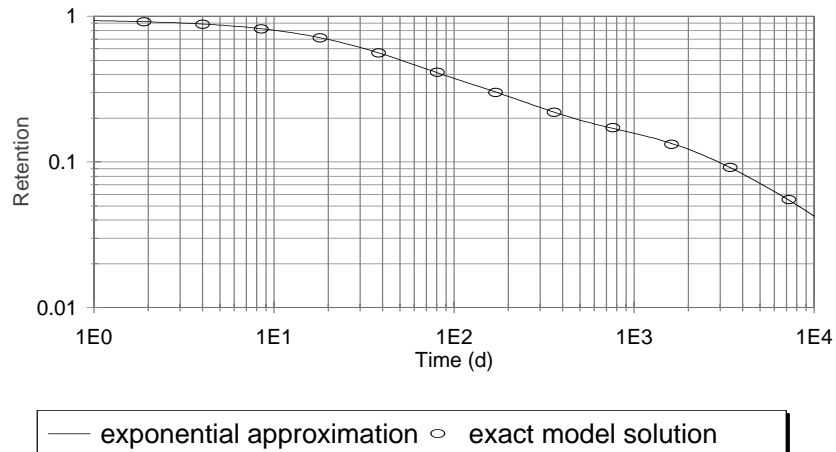
- Systemic retention function.
 In ICRP Publication 54 given for 22 elements

Lead biokinetic model ICRP Publication 67



Comparison of ICRP 67 model with exponential approximation

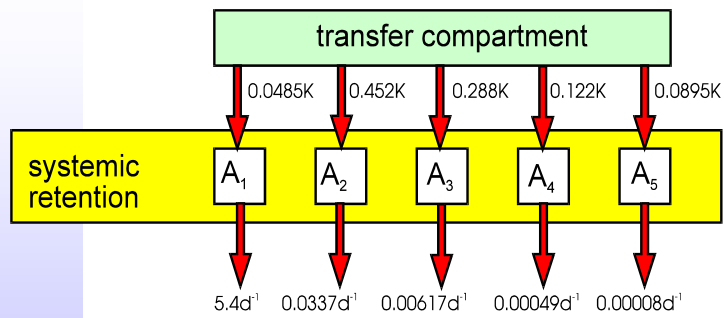
Whole body retention of lead
 (following unit uptake to blood)



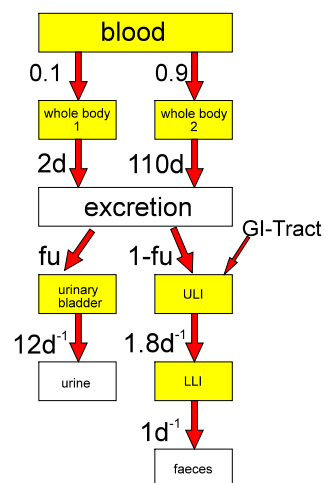
Lead systemic retention function

$$R(t) = 0.0485e^{-5.4t} + 0.452e^{-0.0337t} + 0.122e^{-0.000491t} + 0.0895e^{-0.0000767t} + 0.288e^{-0.00617t}$$

Lead compartment system



Systemic retention of Caesium



Urinary excretion (ICRP 30)

- Retention function $R(t)$ = sum of exponential
- Instantaneous excretion rate obtained by differentiation of systemic retention function
- f_u = fraction of excreted activity to urine

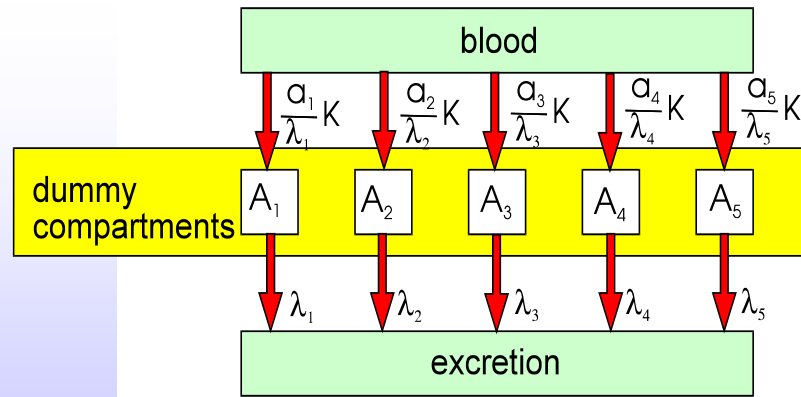
$$\frac{dU}{dt} = -f_u \frac{dR(t)}{dt} = f_u \lambda_i \sum_{i=1}^5 a_i e^{-\lambda_i t}$$

Caesium excretion

- Caesium retention $R(t) = 0.1e^{-\frac{\ln(2)t}{2}} + 0.9e^{-\frac{\ln(2)t}{110}}$
- $f_u = 80\%$
- Urinary excretion

$$\frac{dU}{dt} = 0.08 \frac{\ln(2)}{2} e^{-\frac{\ln(2)t}{2}} + 0.72 \frac{\ln(2)}{110} e^{-\frac{\ln(2)t}{110}}$$

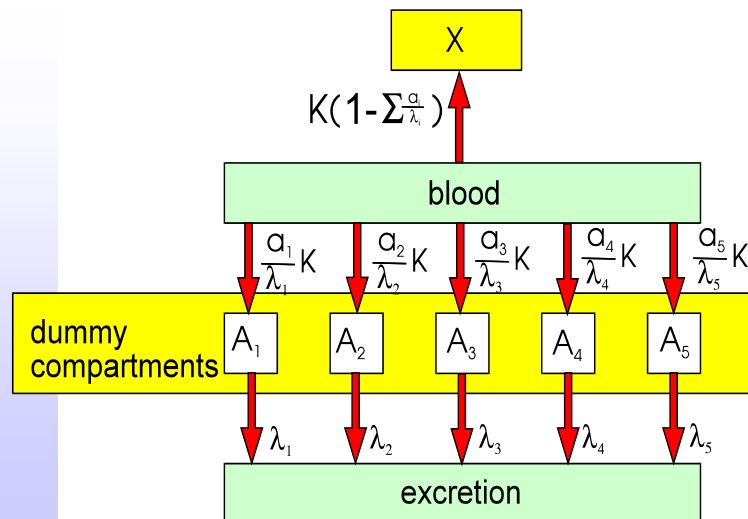
Excretion compartmental representation



Excretion compartmental representation (II)

- K is very fast
- Dummy compartments start with a_i/λ_i amounts
- Instantaneous excretion rate = sum of exponential terms $a_i \exp(-\lambda_i t)$
- Integration, total amount excreted at $t=\infty$, $\Sigma(a_i/\lambda_i)$
- If all material in blood is excreted, $\Sigma(a_i/\lambda_i)=1$
- If material goes to tissue or organ indefinitely retained excreted via a different route
- \Rightarrow an other compartment where $[1 - \Sigma(a_i/\lambda_i)]$ not available for excretion

Excretion compartmental representation (III)



Faecal excretion

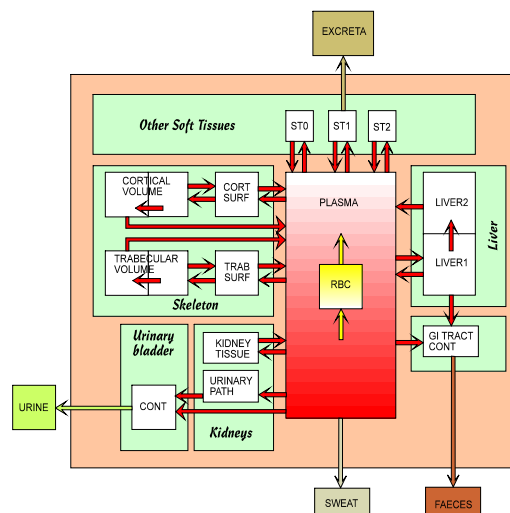
- Faecal excretion comprises 2 components
 - Activity cleared from the lungs by mechanical transport through the HAT
 - Activity in blood extracted by the liver = systemic faecal excretion
- Caesium example: systemic faecal excretion

$$\frac{dF}{dt} = 0.02 \frac{\ln(2)}{2} e^{-\frac{\ln(2)t}{2}} + 0.18 \frac{\ln(2)}{110} e^{-\frac{\ln(2)t}{110}}$$

Urinary excretion rates

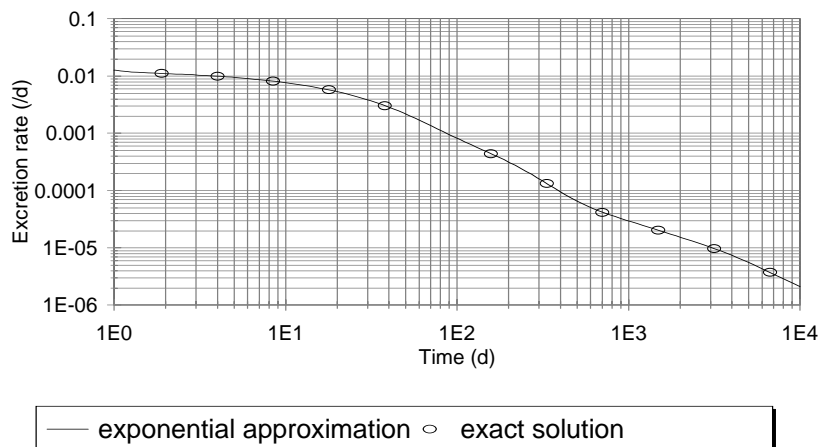
- By differentiation of the retention function
- Not simple with the new models
- Urinary excretion is explicitly in the model
- Calculation of instantaneous urinary excretion rate by:
 - Solving the amount in the urine compartment at times t and $t-\delta t$ and dividing by $(t-\delta t) =$ instantaneous rate as δt tends to 0
 - Solving for the amount in the urinary bladder contents (CONT) at time t and multiplying by the rate constant from CONT to URINE

Lead biokinetic model ICRP Publication 67



Comparison of instantaneous urinary excretion of lead

Instantaneous urinary excretion rate
 (following unit uptake of lead)

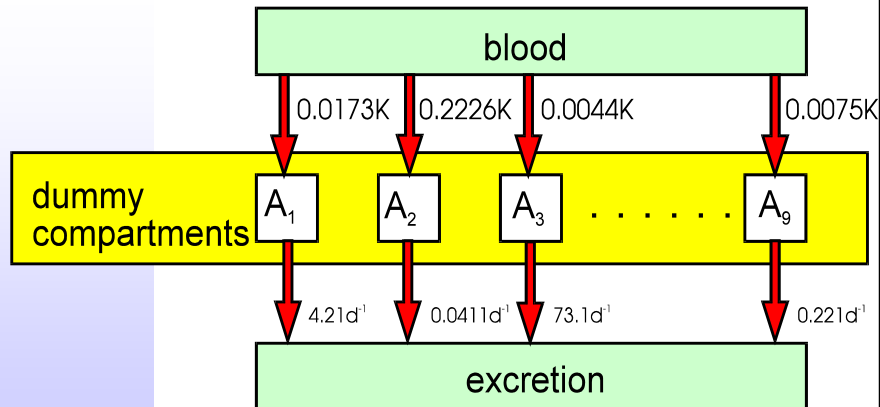


Lead urinary excretion

- Calculate this for 1 to 10⁴ days
- Can fitted a function with sum of exponential
- At t=0, CONT = 0 => Σa_i = 0

$$\frac{dU}{dt} = 0.07264e^{-4.21t} + 0.00915e^{-0.0411t} - 0.327e^{-73.7t} \\
+ 0.242e^{-11t} + 0.00145e^{-0.00901t} + 0.000026e^{-0.000431t} \\
+ 0.00000378e^{-0.0000761t} + 0.0000707e^{-0.00205t} + 0.00166e^{-0.221t}$$

Instantaneous urinary excretion rate of lead



Daily urinary excretion rates

- Can be calculated by either:
 - Integrating the instantaneous excretion rate function from $t-1$ to t
 - Calculating the amount in the excretion compartment at times $t-1$ and t and subtracting one from the other
- To calculate daily excretion rates following inhalation (or ingestion) the respiratory tract and GI tract must be added to the compartment representation and the second calculation option used

Systemic instantaneous faecal excretion rate

$$\frac{dF}{dt} = 0.06073e^{-1.23t} - 0.613e^{-1.26t} + 0.0000262e^{-0.00154t} \\ + 0.00457e^{-0.0277t} + 0.0000139e^{-0.000412t} + 0.00000216e^{-0.000075t} \\ + 0.000595e^{-0.00732t} + 0.00046e^{-44.4t}$$

- Non-systemic component of faecal excretion from material in the GI tract must be added when convoluting with respiratory and GI tract

Suggestion

- Thank you and ...
- What about filling up the Human Alimentary tract.

• ***“Bon appétit”***